

Algebra 1A

Lesson 3.3

Solve Multi - Step Equations

Warm-Up

Simplify.

(a) $2x - 5 + 3x$

$$\begin{array}{r} 2x - 5 + 3x \\ \hline 5x - 5 \end{array}$$

(b) $4x + 3(x - 2) + 1$

$$4x + 3x - 6 + 1$$

$$\begin{array}{r} 4x + 3x - 6 + 1 \\ \hline x + 7 \end{array}$$

(c) $3x - 2(x + 2)$

$$3x - 2x - 4$$

$$\begin{array}{r} 3x - 2x - 4 \\ \hline x - 4 \end{array}$$

(d) $4(x + 3)$

$$4x + 12$$

Steps for Solving

1. Simplify each side of the equal sign (distribute and collect like terms)
2. Use OPPOSITE operations in the OPPOSITE order
3. Give your answer as an $x =$ (or $y =$, $t =$, etc.)

Example 1. Solve an Equation by Combining Like Terms

Solve.

(a) $9x + x - 7 = 13$

$$\begin{array}{r} 9x + x - 7 = 13 \\ +7 \quad +7 \\ \hline 10x = 20 \\ \frac{10x}{10} = \frac{20}{10} \end{array}$$

$$x = 2$$

(b) $9d - 2d + 4 = 32$

$$\begin{array}{r} 9d + 4 = 32 \\ -4 \quad -4 \\ \hline 7d = 28 \\ \frac{7d}{7} = \frac{28}{7} \end{array}$$

$$d = 4$$

Example 2. Solve an Equation by Using the Distributive Property

Solve.

(a) $2w + 3(w + 4) = 27$

$$2w + 3w + 12 = 27$$

$$5w + 12 = 27$$

$$\begin{array}{r} 5w + 12 = 27 \\ -12 \quad -12 \\ \hline 5w = 15 \\ \frac{5w}{5} = \frac{15}{5} \end{array}$$

$$w = 3$$

(b) $4x + 7(x - 2) = 26$

$$4x - 7x + 14 = 26$$

$$\begin{array}{r} 4x - 7x + 14 = 26 \\ -3x + 14 = 26 \\ -14 \quad -14 \\ \hline -3x = 12 \\ \frac{-3x}{-3} = \frac{12}{-3} \end{array}$$

$$x = -4$$

Try It!

Solve.

(a) $11v - 9 - 7v = 15$

$$4v - 9 = 15$$

$$\begin{array}{r} 4v - 9 = 15 \\ +9 \quad +9 \\ \hline 4v = 24 \\ \frac{4v}{4} = \frac{24}{4} \end{array}$$

$$v = 6$$

(b) $14 + 2(4g - 3) = 40$

$$14 + 8g - 6 = 40$$

$$\begin{array}{r} 14 + 8g - 6 = 40 \\ 8 + 8g = 40 \\ -8 \quad -8 \\ \hline 8g = 32 \\ \frac{8g}{8} = \frac{32}{8} \end{array}$$

$$g = 4$$

(c) $6x + 2(x - 5) = 46$

$$6x - 2x + 10 = 46$$

$$\begin{array}{r} 6x - 2x + 10 = 46 \\ 4x + 10 = 46 \\ -10 \quad -10 \\ \hline 4x = 36 \\ \frac{4x}{4} = \frac{36}{4} \end{array}$$

$$x = 9$$

Example 3. Multiply by a Reciprocal to Solve

Solve $\frac{3}{5}(2x-4)=18$.

$$\frac{5}{3} \cdot \frac{3}{5} (2x-4) = 18 \cdot \frac{5}{3}$$

$$\begin{array}{r} 2x-4 = 30 \\ +4 \quad +4 \\ \hline 2x = 34 \\ \frac{2x}{2} = \frac{34}{2} \end{array}$$

$x = 17$

Using the Distributive Property

$$\frac{3}{5} (2x-4) = 18$$

$$(5) \left(\frac{6}{5}x - \frac{12}{5} \right) = (18)(5)$$

$$\frac{6x}{6} = \frac{102}{6}$$

$$\begin{array}{r} 6x - 12 = 90 \\ +12 \quad +12 \end{array}$$

$x = 17$

Example 4. More Multiply by a Reciprocal

Solve $-\frac{4}{5}(4a-1)=28$

$$\left(-\frac{5}{4}\right) \left(-\frac{4}{5}(4a-1)\right) = (28) \left(-\frac{5}{4}\right)$$

$$\begin{array}{r} 4a-1 = -35 \\ +1 \quad +1 \\ \hline 4a = -34 \\ \frac{4a}{4} = \frac{-34}{4} \end{array}$$

$a = -8\frac{1}{2}$

Example 5. Problem Solving

Tickets for a Pistons game can be purchased online through Ticketmaster. For one section at the Palace tickets are \$32.50 for each seat, plus a convenience charge of \$3.30 for each ticket. No matter how many tickets are ordered there is a processing fee of \$5.90. If a customer's total order costs \$220.70, how many tickets did they order?

$$x(32.50 + 3.30) + 5.90 = 220.70$$

$$\begin{array}{r} 35.80x + 5.90 = 220.70 \\ -5.90 \quad -5.90 \\ \hline 35.80x = 214.80 \\ \frac{35.80x}{35.80} = \frac{214.80}{35.80} \end{array}$$

$x = 6$

They ordered
6 tickets
for the
Pistons game.

Assignment: Pages 150 - 151 (4 - 32) even**Review:**

Solve the equation. Show work.

1. $8 - y = -9$

2. $8b = 5$

3. $\frac{3}{4}q = 24$

4. The sum of three numbers is 123. The second number is 9 less than two times the first number. The third number is 6 more than three times the first number. Find the three numbers.

5. The bill (parts and labor) for the repair of a car was \$458. The cost of parts was \$339. The cost of labor was \$34 per hour. Write and solve an equation to find the number of hours of labor.