

Figure 1

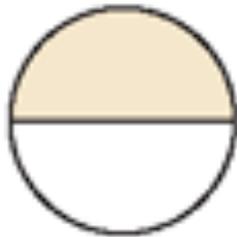


Figure 2

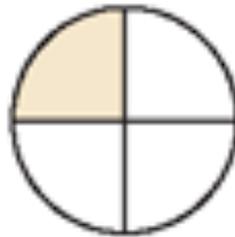
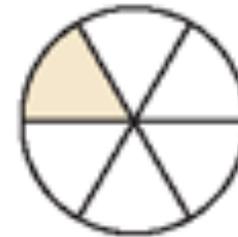
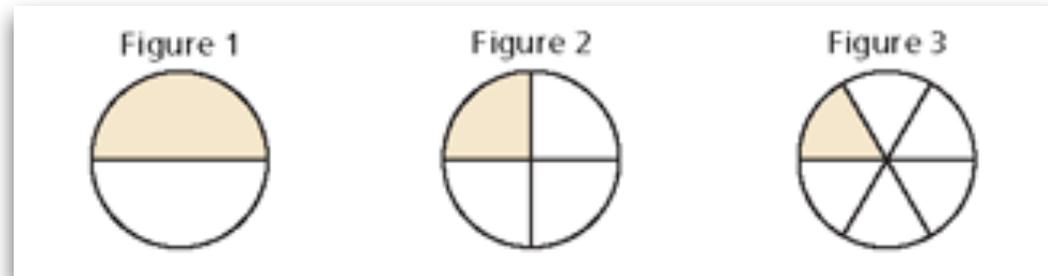


Figure 3



VOCABULARY

- conjecture
- inductive reasoning
- counterexample
- deductive reasoning



LEARNING TARGETS

- I can use inductive reasoning
- I can use deductive reasoning

2.2 Inductive and Deductive Reasoning

Vocabulary: Conjecture and Inductive Reasoning

- A **conjecture** is an unproven statement that is based on observations. You use **inductive reasoning** when you find a pattern in specific cases and then write a conjecture for the general case.

Example

- Numbers such as 3, 4, and 5 are called consecutive integers. Make and test a conjecture about the sum of any three consecutive integers.

Vocabulary: Counterexample

- To show that a conjecture is true, you must show that it is true for all cases. You can show that a conjecture is false, however, by finding just one *counterexample*. A **counterexample** is a specific case for which the conjecture is false.

Example

- A student makes the following conjecture about the sum of two numbers. Find a counterexample to disprove the student's conjecture.
- **Conjecture:** The sum of two numbers is always more than the greater number.

Vocabulary: Deductive Reasoning

- **Deductive reasoning** uses facts, definitions, accepted properties, and the laws of logic to form a logical argument. This is different from inductive reasoning, which uses specific examples and patterns to form a conjecture.

Core Concepts: Laws of Logic

Law of Detachment

If the hypothesis of a true conditional is true, then the conclusion is also true.

Law of Syllogism

If hypothesis p , then conclusion q .

If hypothesis q , then conclusion r .

If these statements are true,

If hypothesis p , then conclusion r .

then this statement is true.

Example

- If two segments have the same length, then they are congruent. You know that $BC = XY$. Using the Law of Detachment, what statement can you make?

Example

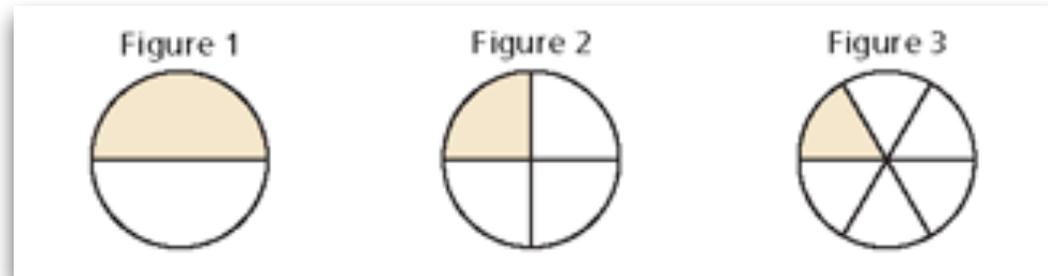
- If possible, use the Law of Syllogism to write a new conditional statement that follows from the pair of true statements.
 - If a polygon is regular, then all angles in the interior of the polygon are congruent
 - If a polygon is regular, then all its sides are congruent.

Example

- If possible, use the Law of Syllogism to write a new conditional statement that follows from the pair of true statements.
 - If $x > 5$, then $x^2 > 25$.
 - If $x^2 > 25$, then $x^2 > 20$.

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